



UNIVERSITY OF SEVILLE
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Cellular programming: efficient resolution of NP-complete numerical problems

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